

**4-5 Study Guide and Intervention****Completing the Square**

**Square Root Property** Use the Square Root Property to solve a quadratic equation that is in the form “perfect square trinomial = constant.”

**Example** Solve each equation by using the Square Root Property. Round to the nearest hundredth if necessary.

**a.**  $x^2 - 8x + 16 = 25$

$$x^2 - 8x + 16 = 25$$

$$(x - 4)^2 = 25$$

$$x - 4 = \sqrt{25} \quad \text{or} \quad x - 4 = -\sqrt{25}$$

$$x = 5 + 4 = 9 \quad \text{or} \quad x = -5 + 4 = -1$$

The solution set is  $\{9, -1\}$ .

**b.**  $4x^2 - 20x + 25 = 32$

$$4x^2 - 20x + 25 = 32$$

$$(2x - 5)^2 = 32$$

$$2x - 5 = \sqrt{32} \quad \text{or} \quad 2x - 5 = -\sqrt{32}$$

$$2x - 5 = 4\sqrt{2} \quad \text{or} \quad 2x - 5 = -4\sqrt{2}$$

$$x = \frac{5 \pm 4\sqrt{2}}{2}$$

The solution set is  $\left\{\frac{5 \pm 4\sqrt{2}}{2}\right\}$ .

**Exercises**

Solve each equation by using the Square Root Property. Round to the nearest hundredth if necessary.

1.  $x^2 - 18x + 81 = 49$

$$\{2, 16\}$$

2.  $x^2 + 20x + 100 = 64$

$$\{-2, -18\}$$

3.  $4x^2 + 4x + 1 = 16$

$$\left\{\frac{3}{2}, -\frac{5}{2}\right\}$$

4.  $36x^2 + 12x + 1 = 18$

$$\left\{\frac{-1 \pm 3\sqrt{2}}{6}\right\}$$

5.  $9x^2 - 12x + 4 = 4$

$$\left\{0, \frac{4}{3}\right\}$$

6.  $25x^2 + 40x + 16 = 28$

$$\left\{\frac{-4 \pm 2\sqrt{7}}{5}\right\}$$

7.  $4x^2 - 28x + 49 = 64$

$$\left\{\frac{15}{2}, -\frac{1}{2}\right\}$$

8.  $16x^2 + 24x + 9 = 81$

$$\left\{\frac{3}{2}, -3\right\}$$

9.  $100x^2 - 60x + 9 = 121$

$$-\{0.8, 1.4\}$$

10.  $25x^2 + 20x + 4 = 75$

$$\left\{\frac{-2 \pm 5\sqrt{3}}{5}\right\}$$

11.  $36x^2 + 48x + 16 = 12$

$$\left\{\frac{-2 \pm \sqrt{3}}{3}\right\}$$

12.  $25x^2 - 30x + 9 = 96$

$$\left\{\frac{3 \pm 4\sqrt{6}}{5}\right\}$$

**4-5 Study Guide and Intervention** *(continued)***Completing the Square**

**Complete the Square** To complete the square for a quadratic expression of the form  $x^2 + bx$ , follow these steps.

1. Find  $\frac{b}{2}$ . → 2. Square  $\frac{b}{2}$ . → 3. Add  $\left(\frac{b}{2}\right)^2$  to  $x^2 + bx$ .

**Example 1** Find the value of  $c$  that makes  $x^2 + 22x + c$  a perfect square trinomial. Then write the trinomial as the square of a binomial.

**Step 1**  $b = 22$ ;  $\frac{b}{2} = 11$

**Step 2**  $11^2 = 121$

**Step 3**  $c = 121$

The trinomial is  $x^2 + 22x + 121$ , which can be written as  $(x + 11)^2$ .

**Example 2** Solve  $2x^2 - 8x - 24 = 0$  by completing the square.

$$2x^2 - 8x - 24 = 0$$

Original equation

$$\frac{2x^2 - 8x - 24}{2} = \frac{0}{2}$$

Divide each side by 2.

$$x^2 - 4x - 12 = 0$$

$x^2 - 4x - 12$  is not a perfect square.

$$x^2 - 4x = 12$$

Add 12 to each side.

$$x^2 - 4x + 4 = 12 + 4$$

Since  $\left(\frac{4}{2}\right)^2 = 4$ , add 4 to each side.

$$(x - 2)^2 = 16$$

Factor the square.

$$x - 2 = \pm 4$$

Square Root Property

$$x = 6 \text{ or } x = -2$$

Solve each equation.

The solution set is  $\{6, -2\}$ .

**Exercises**

Find the value of  $c$  that makes each trinomial a perfect square. Then write the trinomial as a perfect square.

1.  $x^2 - 10x + c$

**25;  $(x - 5)^2$**

2.  $x^2 + 60x + c$

**900;  $(x + 30)^2$**

3.  $x^2 - 3x + c$

**$\frac{9}{4}$ ;  $\left(x - \frac{3}{2}\right)^2$**

4.  $x^2 + 3.2x + c$

**2.56;  $(x + 1.6)^2$**

5.  $x^2 + \frac{1}{2}x + c$

**$\frac{1}{16}$ ;  $\left(x + \frac{1}{4}\right)^2$**

6.  $x^2 - 2.5x + c$

**1.5625;  $(x - 1.25)^2$**

Solve each equation by completing the square.

7.  $y^2 - 4y - 5 = 0$

**-1, 5**

8.  $x^2 - 8x - 65 = 0$

**-5, 13**

9.  $w^2 - 10w + 21 = 0$

**3, 7**

10.  $2x^2 - 3x + 1 = 0$

**$1, \frac{1}{2}$**

11.  $2x^2 - 13x - 7 = 0$

**$-\frac{1}{2}, 7$**

12.  $25x^2 + 40x - 9 = 0$

**$\frac{1}{5}, -\frac{9}{5}$**

13.  $x^2 + 4x + 1 = 0$

**$-2 \pm \sqrt{3}$**

14.  $y^2 + 12y + 4 = 0$

**$-6 \pm 4\sqrt{2}$**

15.  $t^2 + 3t - 8 = 0$

**$\frac{-3 \pm \sqrt{41}}{2}$**